Regents Chemistry:

# Notes: Unit 1: Math and Measurement 



The following 4-Letter Words are forbidden here:
Inch Mile

Foot
Pint Yard

Acre
And we never swear the $\operatorname{Big} \mathbf{F}$ (use ${ }^{\circ} \mathrm{C}$ ) zalease keep it clear and $\mathfrak{A l l}$ etrí

- Major Understandings:
- Chemistry is the study of matter: Matter takes up space and has mass. (K4,3.1a)
- Objects have properties that can be observed, described, and/or measured. (K-4, 3.1c)
- Density can be described as the amount of matter that is in a given amount of space. If two objects have equal volume, but one had more mass, the one with more mass is denser. (5-8, 3.1h)
- SKILLS:

○ Use algebraic and geometric representations to describe and compare data. (M1.1)

- Determine the volume of a regular- and an irregular-shaped solid using water displacement.(5-8, skill PS 11)
- Describe the relationship between mass and volume and compute one variable given the other two.
- Convert temperatures in Celsius degrees ( ${ }^{\circ} \mathrm{C}$ ) to Kelvins (K) and Kelvins to Celsius degrees (3.4iii)

| Word | Definition |
| :---: | :---: |
| Absolute Zero | The theoretical temperature at which all molecular motion stops. This is equal to 0 K or $-273^{\circ} \mathrm{C}$. |
| Accuracy | How close a measured value is to the accepted (or standard) value for that measurement. |
| Celsius | A temperature scale based on the freezing and normal boiling points of water ( 0 and $100^{\circ} \mathrm{C}$, respectively). |
| Control | The conditions with remain constant during an experiment. |
| Conversion Factor | A number or ratio (in fraction form) that is used to convert from one unit type to another. The given units cancel out, leaving the desired target units. |
| Data | That which is measured or observed during an experiment. |
| Density | The relationship between mass and volume, i.e., how "tightly packed" a sample is. $\mathrm{D}=\mathrm{m} / \mathrm{V}$. |
| Dependent Variable | The variable on the Y -axis that changes as a result of changing the independent variable. |
| Experiment | An activity designed to test the specifics of the hypothesis. |
| Exponent | A number that expresses a "power", is written as a superscript. |
| Extrapolation | Extending a graph beyond the data points to predict values beyond that which was plotted to get desired information. |
| Gram | The standard unit of measurement for mass. |
| Hypothesis | An "if-then-because" statement used to design an experiment to test an idea. |
| Independent Variable | The variable on the X-axis that the experimenter has control over. |
| Indirect (or Inverse) Relationship | A relationship where the increase of the independent variable results in the decrease of the dependent variable, or vice versa. |
| Interpolation | Reading between plotted data points on a graph to get desired information. |
| Kelvin | An absolute temperature scale proportional to Celsius but set at $0 \mathrm{~K}=$ absolute zero. |
| Line of Best Fit | A straight line that best represents the slope of the data being analyzed. Can be approximated by hand or done with linear regression methods. |
| Liter | The standard unit of measurement of volume. |
| Mass | A measurement of the amount of matter in a sample. |
| Matter | Anything in nature which has mass and occupies space (has volume). |
| Meniscus | The curve in the surface of a liquid resulting from surface tension with the container. Measurements are made level with the midpoint. |
| Percent Error | A measure of how accurate a measurement is in relation to the actual or accepted value of that measurement. |

Vocabulary

| Precision | The place to which a measurement was made, e.g., ones, tens, tenths |
| :--- | :--- |
| Scientific Notation | A method of writing or displaying numbers in terms of a decimal number <br> between 1 and 10, multiplied by a power of 10. |
| Significant Figures | The number of digits actually recorded by a measuring device during a <br> measurement. |
| Tare | The mass of the receptacle containing the sample. This value is subtracted <br> from the total mass to get the mass of the sample. |
| Temperature | A measurement of the Average Kinetic Energy of a sample. |
| Unit | A symbol which identifies the type of measurement that has been made. This <br> needs to be placed after every measured number and every calculated answer. |
| Variable | The value that changes during an experiment. |
| Volume | A measurement of how much space a sample occupies. |
| Water Displacement | A method to measure the volume of an irregular solid object by determining <br> the difference in volume between a liquid with and without the object <br> submerged. |

## Objectives:

- Chemistry is the study of matter: Matter takes up space and has mass. (K-4, 3.1a)
- Objects have properties that can be observed, described, and/or measured. (K-4, 3.1c)
- Use algebraic and geometric representations to describe and compare data. (M1.1)
- recognize and convert various scales of measurement

What is Chemistry? The study of matter and its changes.
What is MATTER?

Matter can be described through its properties, using terms which are:
QUALITATIVE (sounds like quality): descriptive, non-numerical observations
Examples:

QUANTITATIVE (sounds like quantity): are in the form of NUMBERS and UNITS.
Examples:

Example: Qualitative or Quantitative?
Some properties of a 5 g sample of sodium are listed below:

- Is a soft, silver-colored metal
- Melts at a temperature of 371 K
- Has a density of $0.97 \mathrm{~g} / \mathrm{cm} 3$
- Oxidizes easily in the presence of air
- Has a volume of 5.1 mL

| Qualitative | Quantitative |
| :---: | :---: |
|  |  |
|  |  |
|  |  |

## Quantitative Measurements:

The METRIC SYSTEM (SI): System of measurement used in science and in most countries The BASE UNITS of measurement: (Found on Reference Table D)

Which units are new to you?

## Example:

Name the quantity measured using Pa.

| Table D <br> Selected Units |  |  |
| :--- | :--- | :--- |
| Symbol | Name | Quantity |
| m | meter | length |
| g | gram | mass |
| Pa | pascal | pressure |
| K | kelvin | temperature |
| mol | mole | amount of <br> substance |
| J | joule | energy, work, <br> quantity of heat |
| s | second | time |
| min | minute | time |
| h | hour | time |
| d | day | time |
| y | year | time |
| L | liter | volume |
| Ppm | parts per million | concentration |
| M | molarity | solution <br> concentration |
| u | atomic mass unit | atomic mass |

PREFIXES: Used to modify base units of measurement. (Found on Reference Table C)
Table C
Selected Prefixes

| Factor | Prefix | Symbol |
| :---: | :---: | :---: |
| $10^{3}$ | kilo- | k |
| $10^{-1}$ | deci- | d |
| $10^{-2}$ | centi- | c |
| $10^{-3}$ | milli- | m |
| $10^{-6}$ | micro- | $\mu$ |
| $10^{-9}$ | nano- | n |
| $10^{-12}$ | pico- | p |

## Which prefixes are you already familiar with?

## Example:

Which prefix would you use for one thousand meters?

Which would you use for one-thousandth of a meter?.

Example: gram (g) is a base unit for mass, while kg is a kilogram, or $10^{3}(1000)$ grams. A unit symbol often consists of both the base unit and a prefix, e.g., $\mathrm{cm}, \mathrm{mL}, \mathrm{kg}$.

## Try these:

Symbol for kiloJoules:
Name unit represented by ms:
Name quantity represented by ms:

## CONVERTING UNITS USING TABLE C

STEP 1: Find the number of places to move the decimal point by finding the difference between the exponents of the two prefixes on Table C.

STEP 2: Determine the direction of movement (left or right).

Move the decimal to the LEFT when going from: SMALLER to LARGER unit
Move the decimal to the RIGHT when going from: LARGER to SMALLER unit
Table C
Selected Prefixes

| Factor | Prefix | Symbol |
| :---: | :---: | :---: |
| $10^{3}$ | kilo- | k |
| $10^{-1}$ | deci- | d |
| $10^{-2}$ | centi | c |
| $10^{-3}$ | milli | m |
| $10^{-6}$ | micro- | $\mu$ |
| $10^{-9}$ | nano- | n |
| $10^{-12}$ | pico- | p |

Larger the unit, the smaller the value, e.g., 5 km

Smaller the unit, the larger the value, e.g, $5,000,000 \mathrm{~mm}$

EXAMPLE 1: Convert 45 mL to L .

- mL is $\qquad$ ; L (base unit) is $\qquad$
The difference between the two factors is $\qquad$ .
- Since you are moving from a smaller prefix to a larger prefix you move the decimal three places to the left.

$$
45 \mathrm{~mL}=
$$

$\qquad$ L (larger unit, smaller value)

## Unit 1: Lesson 1: Measurement \& Metric Conversions

EXAMPLE 2: $5.2 \mathrm{~cm}=$ $\qquad$ mm

- Step 1: Find the difference between the two factors:
- Step 2: Which direction do you move the decimal point?

Final answer: $\qquad$

## Workspace for Video Questions and additional notes:

## Objective:

- Differentiate between Kelvin and Celsius scales
- Convert temperatures in Celsius degrees ( ${ }^{\circ} \mathrm{C}$ ) to Kelvins (K) and Kelvins to Celsius degrees (3.4iii)

What is Temperature?

## Celsius Scale:

- Freezing point of water at $0^{\circ} \mathrm{C}$.
- Boiling for water at $100^{\circ} \mathrm{C}$.
- Below 0 is NEGATIVE.


## Kelvin Scale:

- Water freezes at 273 K and boils at 373 K
- Theoretical point of ABSOLUTE ZERO is when all molecular motion stops ( $0 \mathrm{~K}=-273^{\circ} \mathrm{C}$ )
- NO NEGATIVE NUMBERS
- Divisions (degrees) are the same as in Celsius



# Unit 1 Math \& Measurement: Lesson 3- Temperature Conversions 

## CONVERTING BETWEEN TEMPERATURE SCALES

Temp Conversion Formula:
(TABLE T)

$$
\mathrm{K}={ }^{\circ} \mathrm{C}+273
$$

EXAMPLE 1: What is the temperature in Kelvin of an object that is $55^{\circ} \mathrm{C}$ ?

EXAMPLE 2: What is the temperature in Celsius of an object that is $150 . \mathrm{K}$ ?

EXAMPLE 3: What is the CHANGE in Kelvin if the change in temperature in Celsius goes from $30 .{ }^{\circ} \mathrm{C}$ to $50 .{ }^{\circ} \mathrm{C}$ ?

## Unit 1 Math \& Measurement:

Lesson 4- Measurement Accuracy (Percent Error)

## Objective:

- Differentiate between accuracy and precision
- Compare the experimental result to the expected result; calculate the percent error (S3.3)

ACCURACY - how close a measurement is to the accepted or true value
PRECISION - The place to which a measurement was made, e.g., ones, tens, tenths
EXAMPLE: These students were asked to determine the density of sucrose. Sucrose has a density of $1.59 \mathrm{~g} / \mathrm{cm}^{3}$. Which student is most accurate?

|  | Student A <br> $\left(\mathbf{g} / \mathbf{c m}^{\mathbf{3}} \mathbf{)}\right.$ | Student B <br> $\left(\mathbf{g} / \mathbf{c m}^{\mathbf{3}} \mathbf{)}\right.$ | Student $\boldsymbol{C}$ <br> $\left(\mathbf{g} / \mathbf{c m}^{\mathbf{3}} \mathbf{)}\right.$ |
| :--- | :--- | :--- | :--- |
| Trial 1 | 1.54 | 1.40 | 1.70 |
| Trial 2 | 1.60 | 1.68 | 1.69 |
| Trial 3 | 1.57 | 1.45 | 1.71 |
| Avg. | 1.57 | 1.51 | 1.70 |

## PERCENT ERROR

Measurement of ACCURACY (the \% that the measured value is "off" from accepted value)
Measured value = value you "get"
Accepted value $=$ value you "should get"

Formula located on: TABLE T

| Percent Error | \% error $=\frac{\text { measured value }- \text { accepted value }}{\text { accepted value }} \times 100$ |
| :--- | :--- |

If answer is negative, your measured value is LESS THAN the accepted value
If answer is positive, your measured value is GREATER THAN the accepted value

## Unit 1 Math \& Measurement: <br> Lesson 4- Measurement Accuracy (Percent Error)

EXAMPLE: A student determines the density of a substance to be $1.40 \mathrm{~g} / \mathrm{mL}$. Find the \% error if the accepted value of the density is $1.36 \mathrm{~g} / \mathrm{mL}$.

Percent error has no unit. Why?

## Objective:

- Show uncertainty in measurement by the use of significant figures
- Properly apply rules of significant figures (determining number of significant figures in a measurement).


## SIGNIFICANT FIGURES

Sig Figs Indicate PRECISION of a measurement.

- Recording Sig Figs:
-Sig figs in a measurement include the known digits plus a final estimated digit (precision of instrument)



## EXAMPLE 1:


-We know for sure that the object is more than $\qquad$ cm, but less than $\qquad$ cm
-We know for sure that the object is more than $\qquad$ cm, but less than $\qquad$ cm
-This ruler allows us to estimate the length to $\qquad$ cm

EXAMPLE 2:


Device is marked to the TENS place, so read to the ONES place Measurement: $6 \underline{7} \mathrm{~cm} \leftarrow$ the $\mathbf{7}$ in the ones place is ESTIMATED


Device is marked to the TENTHS place, so read to the HUNDREDTHS place Measurement: $0.4 \underline{8} \mathrm{~cm} \leftarrow$ the 8 in the hundredths place is ESTIMATED

Which measuring tool above is more precise?

Review of the decimal positions -- memorize if you don't know these!!!

| Thousands |
| ---: | :--- | :--- | :--- | :--- |
| Hundreds |
| Tens |
| Ones |

## EXAMPLE 3:

If the graduated cylinder is marked to the ONES, read to the $\qquad$ .

$$
\text { Volume }=\ldots \ldots \mathrm{mL}
$$



EXAMPLE 4: Reading a thermometer marked to the $\qquad$ place, so read to the $\qquad$ .


## RULES FOR COUNTING SIG FIGS

1. All non-zero digits are significant.
2. Leading zeros are never significant.
ex. 0.421 ( 3 sig figs)
3. All captive zeros are always significant.
(Captive is a zero between 2 other non-zero digits.) ex. 4012 (4 sig figs)
4. For Trailing zeros: (zeros after last non-zero digit) sometimes significant...

| - Decimal point $\rightarrow$ significant | ex. 114.20 (5 sig figs) |
| :--- | :--- |
| -No decimal point $\rightarrow$ not significant | ex. 11,420 (4 sig figs) |

## HOW TO COUNT SIG FIGS

1. Start counting from LEFT to RIGHT at first nonzero number.
2. If decimal point is present then count any trailing zeros
3. If decimal is not present don't count trailing zeros

EXAMPLES:

1) 2545.300 g $\qquad$ sig figs (Rule applied: $\qquad$
2) 4530 km $\qquad$ sig figs (Rule applied: $\qquad$
3) 0.00453 m $\qquad$ sig figs (Rule applied: $\qquad$

## Objective:

- Properly apply rules of significant figures (determine number of significant figures to be rounded to when doing calculations).

Every measurement has some error in it. When performing calculations AN ANSWER CAN NEVER BE MORE PRECISE THAN THE LEAST PRECISE MEASUREMENT

## RULES FOR ADDITION/SUBTRACTION

Answer can only be as precise as least precise number.
Example: $15.34 \mathrm{~g}+.028 \mathrm{~g}$-- which is less precise?
Round your answer to which place? $\qquad$ 15.34 g

Final answer: $\qquad$ g

EXAMPLE: $224 \mathrm{~g}+130 \mathrm{~g}=$

EXAMPLE: $24.533 \mathrm{~mL}+34.1 \mathrm{~mL}=$

## RULES FOR MULTIPLICATION/DIVISION

Multiply/Divide - Round answer to the least number of significant figures.
EXAMPLE:


324 g
Example:
$\mathrm{d}=56.0 \mathrm{~g} / 12.45 \mathrm{~mL}$

## Quantitative Calculations:

Mass: the amount of matter an object contains. (This is different than weight, which is mass times gravity)

Volume: The amount of space a substance occupies

How do we measure mass in the lab? The electronic balance.

How can we measure volume?

## 1.) $l \times w \times h$ (regular solid)

$$
\mathrm{ex} . \mathrm{V}=1 \mathrm{~cm}^{3}
$$



## 2.) Graduated cylinder (liquids)

Read bottom of MENISCUS
$e x . V=27.5 \mathrm{~mL}$

3.) Water Displacement: measures volume of an irregular solid

## STEPS TO MESASURE VOLUME BY DISPLACEMENT:

1. Measure initial volume
2. Measure final volume with object
3. The Difference is the volume of the object

EXAMPLE: What is the volume of the solid object?


## CALCULATING DENSITY

## DENSITY: The Ratio of mass of an object to its volume

The density formula is: $\quad d=\frac{m}{V}$ and is located on TABLE T
NOTE: IN WORKING EXAMPLES, BE SURE TO INCLUDE THE FORMULA, VARIABLES, NUMERICAL SET-UP, AND ANSWER WITH UNITS!

EXAMPLE 1:

What is the density of an object with a mass of 60 g and a volume of $2 \mathrm{~cm}^{3}$ ?

EXAMPLE 2:
An object has a volume of $825 \mathrm{~cm}^{3}$ and a density of $13.6 \mathrm{~g} / \mathrm{cm}^{3}$. Find its mass.

How to solve for mass or volume if density is not given:
Use TABLE S to find the density of the element. Then solve for the unknown variable.
EXAMPLE 3:
The volume of an aluminum sample is $251 \mathrm{~cm}^{3}$. What is the mass of the sample?
The density of aluminum on table $S$ is $2.70 \mathrm{~g} / \mathrm{cm}^{3}$

## Unit 1 Math \& Measurement: Lesson 2- Density

EXAMPLE 4:
What is the volume of a 25 g sample of copper?

## WORKSPACE FOR ADDITIONAL NOTES/QUESTIONS:

## Objective:

- Properly use and interpret scientific notation:
- Convert numbers into scientific notation and standard notation
- Compute operations using scientific notation

Scientific notation: A way to represent large or small numbers
For example:

- the mass of a hydrogen atom is 0.00000000000000000000000167 g .
$\cdot 2 \mathrm{~g}$ of $\mathrm{H}_{2}$ contains $602,000,000,000,000,000,000,000$ molecules.
Scientific Notation is written as the product of two numbers: a coefficient and a 10 raised to a power.

The coefficient (number written first) is always a number from 1 to 9
Example (from above):
Mass of a Hydrogen atom is $1.67 \times 10^{-24} \mathrm{~g}$.
2 g of $\mathrm{H}_{2}$ contains $6.02 \times 10^{23}$ molecules.
NOTE: When done correctly, EVERY digit in the coefficient in scientific notation is significant!

## CONVERTING FROM STANDARD NOTATION INTO SCIENTIFIC NOTATION

1. For large numbers (greater than 1) move decimal to the LEFT until there is only 1 digit to its left. The number of places moved $=$ exponent number

EXAMPLE: 454,500 g =
2. For small numbers (less than 1) move decimal to RIGHT stopping after the first non-zero number. The number of places moved = negative exponent number

EXAMPLE: $0.00453 \mathrm{ml}=$

## Unit 1 Math \& Measurement: Lesson 7 - Scientific Notation

## CONVERTING FROM SCIENTIFIC NOTATION INTO STANDARD NOTATION

Move the decimal place the number of times indicated by the exponent:
If exponent is positive, move to the right (number gets larger).
If the exponent is negative, move to the left (number gets smaller).

EXAMPLE:
$4.5 \times 10^{-2}=$

EXAMPLES Convert the following in standard notation:
$6.5678 \times 10^{7}=$
$8.79 \times 10^{-4}=$

## CALCLUATING WITH SCIENTIFIC NOTATION USING A CALCULATOR <br> $3 \times\left(7.04 \times 10^{8} y\right)$

Scientific:
Four-Function:
Type on your calculator:
$3 \quad \mathrm{x} 7.04$
$=2.112 \mathrm{E} 9$
$=2.112 \times 10^{9} \mathrm{y}$
$=2112000000 \mathrm{y}$

## Objective:

- Construct and interpret a graph from experimentally obtained data (M2.1)
- identify independent and dependent variables
- create appropriate axes with labels and scale
- identify graph points clearly
- Identify relationships within variables from graphs (direct, inverse)
- Make predictions using graphs

Graphs are used to visually make sense of experimental data and can also be used to make predictions.

Data Set: An experimenter recorded the temperature of a sample as she added heat over time:

| Time (min) | Temperature <br> $\left({ }^{\circ} \mathrm{C}\right)$ |
| :--- | :--- |
| 0 | 15 |
| 1.0 | 19 |
| 2.0 | 26 |
| 3.0 | 30 |
| 4.0 | 36 |
| 5.0 | 39 |

## Variables:

Changing one thing in an experiment (independent variable) will often cause something else to change (dependent variable).

When graphing, the independent variable is on the X axis (with units) and the dependent variable is on the Y axis (with units).

In this example,
$\qquad$ is independent variable, X -axis
$\qquad$ is dependent variable, Y -axis

| Time (min) | Temperature <br> $\left({ }^{\circ} \mathrm{C}\right)$ |
| :--- | :--- |
| 0 | 15 |
| 1.0 | 19 |
| 2.0 | 26 |
| 3.0 | 30 |
| 4.0 | 36 |
| 5.0 | 39 |

SAMPLE GRAPH (USE A PENCIL AND RULER!):

| Time (min) | Temperature <br> $\left({ }^{\circ} \mathrm{C}\right)$ |
| :--- | :--- |
| 0 | 15 |
| 1.0 | 19 |
| 2.0 | 26 |
| 3.0 | 30 |
| 4.0 | 36 |
| 5.0 | 39 |



1) Label the X - and Y-axes. Don't forget units!!
2) A numerical scale representing uniform increases in each variable.
3) A title: (Dependent Variable) vs. (Independent Variable) or " $y$ " vs. " $x$ "
4) Data points, circled with "point protectors". These circles serve two purposes: to make the point more visible and to represent the margin of error associated with estimated digits.
5) A line either connecting the data points or in a curve of best fit between the points.

NOTE: A computer can draw a very precise, "best fit" - your eyeball is approximate and may differ slightly from your classmates while both are correct!!

Best Fit Line (Average Line): Notice how the line of best fit gives approximately the same number of data points above and below it, while maintaining a good idea of the slope of the data? Use a ruler and a pencil to create this line of best fit. GRAPHS SHOULD ALWAYS BE DONE WITH A PENCIL AND A RULER.

What if you were graphing the temperature change of two different substances you'd have two data sets using the same independent variable - You can use colors or symbols to distinguish, but include a KEY.

## USING YOUR GRAPH:

Interpolation and Extrapolation: When data is graphed and a line drawn, one can make estimations about information that is either between data points or outside the range of the data points.

INTERPOLATION: Reading between the data points to get information.
Examples (Use your sample graph, page 25!):
What will the temperature of the sample be after 2.5 min ? $\qquad$
How long would it take the sample to reach $25^{\circ} \mathrm{C}$ ? $\qquad$
EXTRAPOLATION: Extending your graph line and reading outside your data range.
NOTE: This is a bit more dicey than interpolation as the situation can change, for example, if we're heating water, it will boil at $100 .{ }^{\circ} \mathrm{C}$, so the trend probably won't continue!!

Examples (Use your sample graph, page 25!):
What will the temperature of the sample be after 6.0 min ? $\qquad$
How long would it take the sample to reach $47 .{ }^{\circ} \mathrm{C}$ ? $\qquad$

When you do either, you must keep the rules of precision in mind. If your graph reads to the nearest tenths, the estimated interpolation or extrapolation must be read to the nearest hundredth.


Relationships: Graphs show relationships between the dependent and the independent variable. This can be used to make predictions about behavior of physical and chemical phenomena.

Direct Relationship: As the independent variable is increased, the dependent variable also increases.

Indirect (Inverse) Relationship: As the independent variable is increased, the dependent variable decreases.


As the heat is added over time (increased) the temperature increases. This is a relationship.

As the pressure on a sample of confined gas is increased, its volume will decrease. This is an

## A Good Graph



1) Labeled Axes: dependent on the $Y$ axis, independent on the $X$ axis, both with appropriate units
2) Title: Dependent Variable vs. Independent Variable
3) Data Points: with point protectors around them
4) Best Fit Line: showing the average slope of the linear data
5) Scaled: regular interval spacing for the scales on both axes
6) Size: The data should take up more than a quarter of the graph paper itself. The larger the graph, the easier it is to interpolate and extrapolate from

## If you are not told to draw a best fit line, then connecting the data points individually is the way to go.

